

FUNDAMENTALS OF ENGINEERING

CIVIL EXAM TOPICS

Computer-Based Test (CBT)

Total Number of Questions: 110

Time: 6 hours

The new Civil FE Computer-Based Test (CBT) consists of 110 multiple-choice questions (Each problem only one question) the examinee will have 6 hours to complete the test.

- **Mathematics (Approx. 9 questions*)**
- **Probability and Statistics (5 questions)**
- **Computational Tools (5 questions)**
- **Ethics and Professional Practice (5 questions)**
- **Engineering Economics (5 questions)**
- **Statics (9 questions)**
- **Dynamics (5 questions)**
- **Mechanics of Materials (9 questions)**
- **Civil Engineering Materials (5 questions)**
- **Fluid Mechanics (5 questions)**
- **Hydraulics and Hydrologic Systems (10 questions)**
- **Structural Analysis (8 questions)**
- **Structural Design (8 questions)**
- **Geotechnical Engineering (12 questions)**
- **Transportation Engineering (10 questions)**
- **Environmental Engineering (8 questions)**

* Here the number of questions are the average values taken from the NCEES Reference Handbook (Version 9.1 / Computer-Based Test)


ROOTS OF EQUATIONS

MATHEMATICS

NCEES Reference Handbook / Page-265

$$F(x) = \frac{x^3 + 4x^2 + x - 6}{x + 2}$$

The roots of the above function $F(x)$ are most nearly

- (A) +1, -2, +3
- (B) -1, +2
-  (C) +1, -3
- (D) +1, +2, -3

Solution:

After factoring and simplification:

$$F(x) = \frac{(x-1)(x \cancel{+2})(x+3)}{(x \cancel{+2})}$$

$$(x-1)(x+3)=0$$

$$\text{First Root} = +1$$

$$\text{Second Root} = -3$$

ROOTS OF EQUATIONS

MATHEMATICS

NCEES Reference Handbook / Page-265

(1)
$$F(x) = \frac{x^3 - 2x^2 - 5x + 6}{x - 3}$$

The roots of the above function $F(x)$ are most nearly

- (A) +1, -2, +3
- (B) -1, +2
- (C) +1, -2
- (D) +1, +2, -3

(2)
$$F(x) = \frac{x^3 + 3x^2 - 10x - 24}{x + 4}$$

The roots of the above function $F(x)$ are most nearly

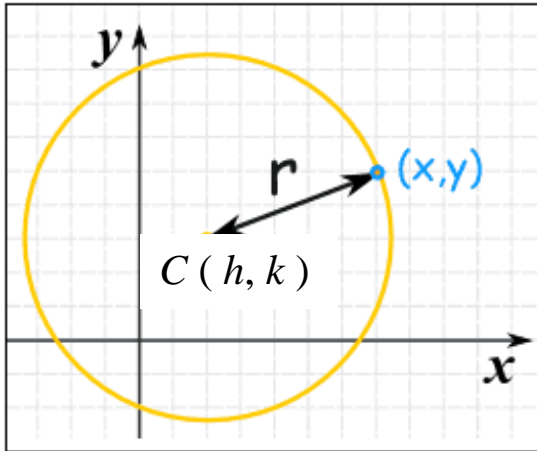
- (A) +1, -2
- (B) -2, +3
- (C) +3, -4
- (D) +2, -3, +4

FUNDAMENTALS OF ENGINEERING

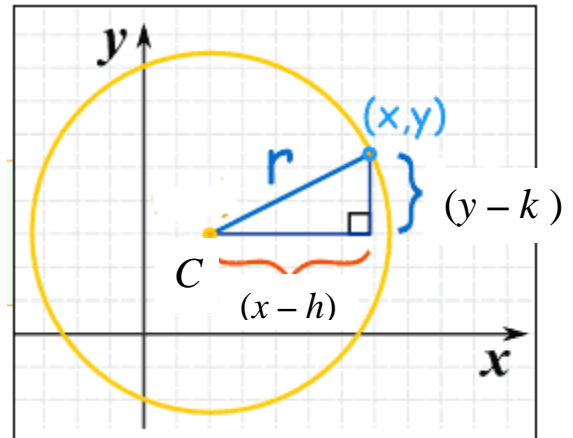
DOMAIN: MATHEMATICS

CIRCLE EQUATIONS

(NCEES-Ref Handbook / Page-23)



Center: $C(h, k)$



Radius: r

Standard form of a Circle Equation:

$$(x - h)^2 + (y - k)^2 = r^2$$

$$r = \text{SQRT} (x - h)^2 + (y - k)^2$$

Example:

The equation of a circle with center at $C(-7, 9)$ and a radius of 5 is:

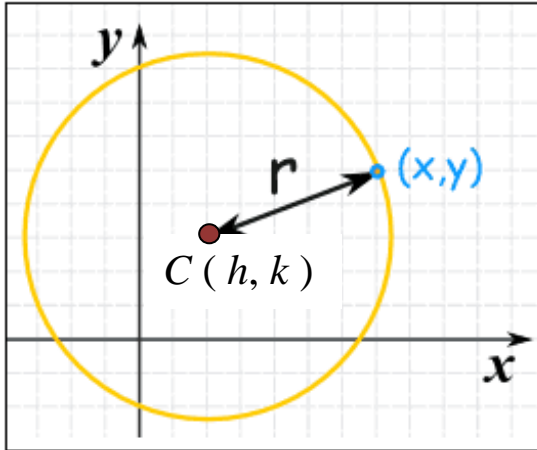
- (A) $(x - 7)^2 + (y - 9)^2 = 5$
- (B) $(x + 7)^2 + (y - 9)^2 = 5$
- (C) $(x - 7)^2 + (y + 9)^2 = 25$
- ⇒ (D) $(x + 7)^2 + (y - 9)^2 = 25$

FUNDAMENTALS OF ENGINEERING

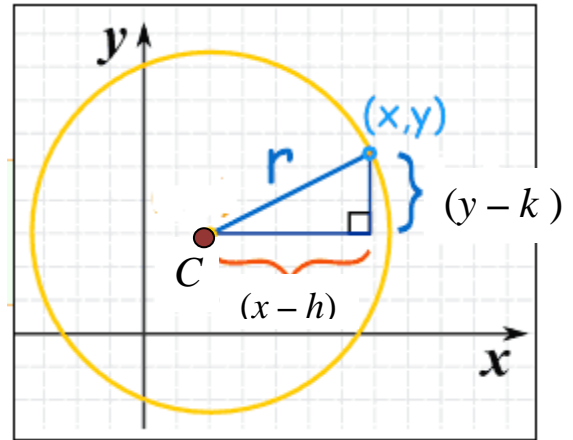
DOMAIN: MATHEMATICS

EQUATION OF A CIRCLE

(NCEES-Ref Handbook / Page-23)



Center: $C(h, k)$



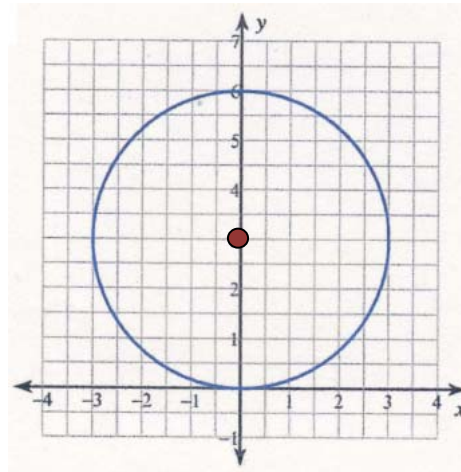
Radius: r

Standard form of Equation of a Circle

$$(x - h)^2 + (y - k)^2 = r^2$$

$$r = \text{SQRT} (x - h)^2 + (y - k)^2$$

Example:



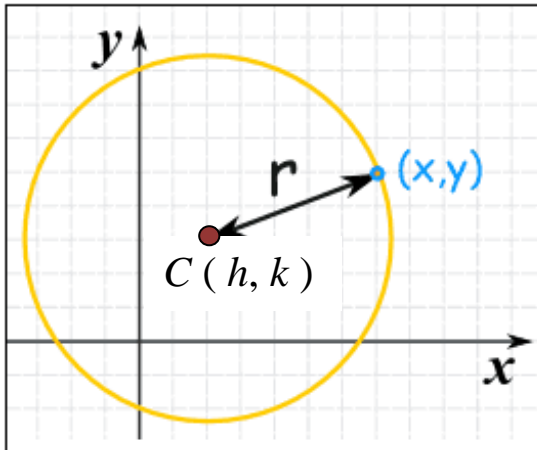
$$x^2 + (y - 3)^2 = 9$$

FUNDAMENTALS OF ENGINEERING

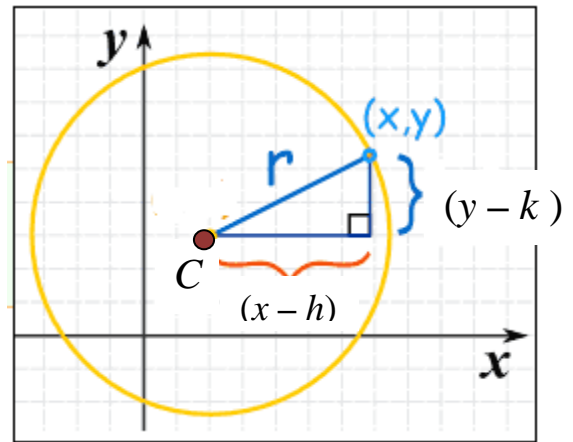
MATHEMATICS

EQUATION OF A CIRCLE (Standard Form)

NCEES-Reference Handbook / Page-23



Center: $C(h, k)$



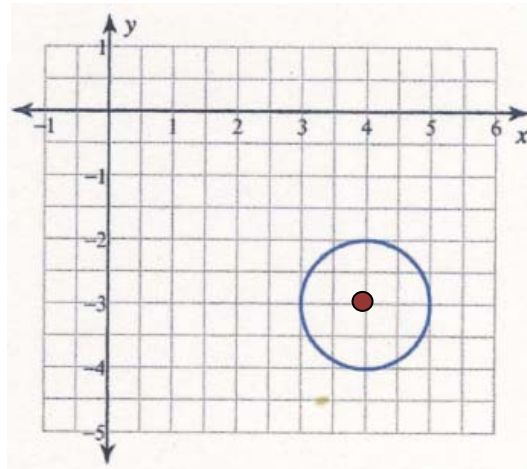
Radius: r

Standard form of Equation of a Circle

$$(x - h)^2 + (y - k)^2 = r^2$$

$$r = \text{SQRT} (x - h)^2 + (y - k)^2$$

Example:



Center: $C(4, -3)$


$$(x - 4)^2 + (y + 3)^2 = 1$$

Problem: (Matrix Algebra)

$$\mathbf{A} = \begin{bmatrix} 3 & -3 & 2 \\ 2 & 5 & -3 \\ 3 & -1 & 1 \end{bmatrix}$$

Using the matrix given above, answer the following questions:

(1) the determinant of the above matrix is most nearly


- (A) 4
-  (B) 5
- (C) 6
- (D) 8

(2) the inverse of matrix \mathbf{A} is most nearly, (\mathbf{A}^{-1})

(A)
$$\mathbf{A}^{-1} = \begin{bmatrix} 1/4 & 1/4 & -1/4 \\ 10/4 & 5/4 & 13/4 \\ -10/4 & -4/4 & 11/4 \end{bmatrix}$$

(B)
$$\mathbf{A}^{-1} = \begin{bmatrix} 2/3 & 1/3 & -1/6 \\ -11/3 & -7/3 & 13/3 \\ -17/3 & -8/3 & 32/3 \end{bmatrix}$$

(C)
$$\mathbf{A}^{-1} = \begin{bmatrix} 2/5 & 1/5 & 1/5 \\ 11/5 & 3/5 & 13/5 \\ -17/5 & -6/5 & 21/5 \end{bmatrix}$$

 (D)
$$\mathbf{A}^{-1} = \begin{bmatrix} 2/5 & 1/5 & -1/5 \\ -11/5 & -3/5 & 13/5 \\ -17/5 & -6/5 & 21/5 \end{bmatrix}$$

FUNDAMENTALS OF ENGINEERING

DOMAIN: MATHEMATICS

MATRICES & DETERMINANTS

NCEES-Reference Handbook / Pages 30-31

$$\mathbf{A} = \begin{bmatrix} 2 & -3 \\ 1 & -1 \end{bmatrix}$$

$$\mathbf{B} = \begin{bmatrix} 1 & 2 & -0 \\ 2 & -5 & -2 \end{bmatrix}$$

Using the matrices given above, answer the following questions:

(1) the determinant of the matrix **A** is most nearly

- (A) 4
- (B) -3
- (C) -2
- (D) 1

(2) the matrix product of **A** and **B** is most nearly, **A*B**

(A) $\mathbf{A*B} = \begin{bmatrix} -4 & 12 & -10 \\ 2 & -5 & -2 \end{bmatrix}$

(B) $\mathbf{A*B} = \begin{bmatrix} -1 & 12 & -4 \\ 0 & -5 & -2 \end{bmatrix}$

(C) $\mathbf{A*B} = \begin{bmatrix} -4 & 19 & 6 \\ -1 & 7 & 2 \end{bmatrix}$

(D) $\mathbf{A*B} = \begin{bmatrix} -2 & 11 & -20 \\ 2 & 13 & 7 \end{bmatrix}$

FUNDAMENTALS OF ENGINEERING

ENGINEERING ECONOMICS

Problem: (Compound Interest)

A sum of \$10,000 is deposited in a savings account and left there to earn interest for 10 years. If the interest rate per year is 8% the compound amount after 10 years is most nearly:

- (A) 18, 546
- (B) 21,589
- (C) 24,576
- (D) 27,368

$$F = ?$$

NCEES - Ref. Handbook
Page 132, Factor Table
 $i = 8.00 \%$

Problem: (Compound Interest)

A student wants to pay off a current debt of \$2,500 in three years. Knowing that the interest rate is 6 % compounded annually, the amount that must be paid at the end of the third year is most nearly:

- (A) 3,254
- (B) 3,152
- (C) 2,978
- (D) 2,874

$$F = ?$$

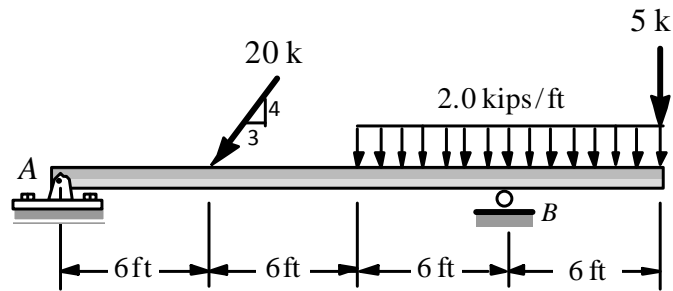
NCEES - Ref. Handbook
Page 131, Factor Table
 $i = 6.00 \%$

FUNDAMENTALS OF ENGINEERING

STATICS

BEAM SUPPORT REACTIONS

NCEES-Reference Handbook / Page-63



A determinate beam is loaded as shown. Knowing that A is a pin support and B is a roller, answer the following questions:

(1) The horizontal support reaction (kips) at A is most nearly:

- (A) 10.00
- (B) 11.25
- (C) 12.00
- (D) 15.00

$$A_x = ?$$

(2) The vertical support reaction (kips) at B is most nearly:

- (A) 48.55
- (B) 44.00
- (C) 42.30
- (D) 36.00

$$B_y = ?$$

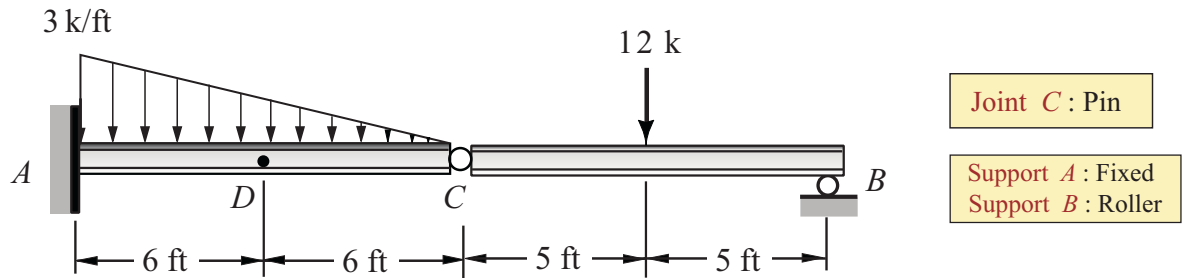
(3) The vertical support reaction (kips) at A is most nearly:

- (A) 8.00
- (B) 9.00
- (C) 10.50
- (D) 12.30

$$A_y = ?$$

BEAMS WITH INTERNAL HINGES

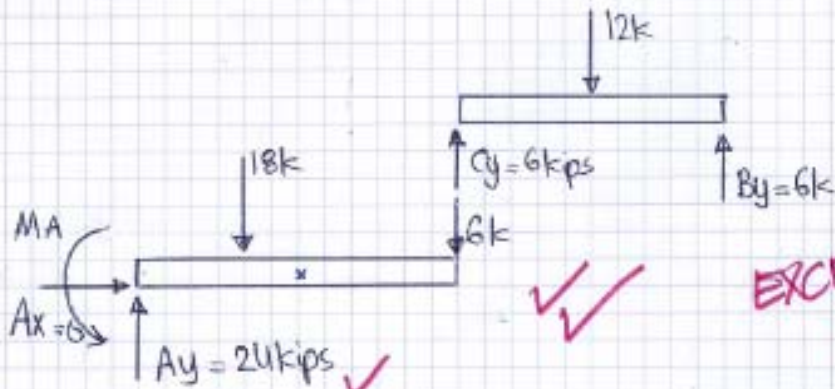
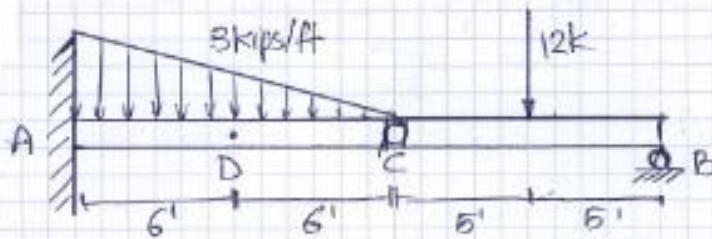
DOMAIN: STATICS



Two beams are connected with an internal pin at C as shown. Using the given loads and the support conditions, determine the following:

- (1) the vertical support reaction (kips) at support B
 - (A) 4.50
 - (B) 4.75
 - (C) 5.00
 - (D) 6.00
- (2) the bending moment (ft-kips) at support A
 - (A) 238
 - (B) 214
 - (C) 144
 - (D) 124
- (3) the bending moment (ft-kips) at point D
 - (A) 48
 - (B) 45
 - (C) 36
 - (D) 30

BEAMS WITH INTERNAL HINGES



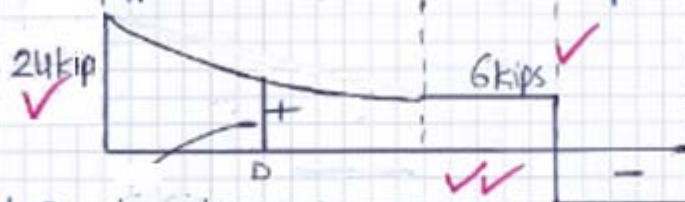
EXCELLENT!

$$\begin{aligned} \sum \circlearrowleft M_B = 0 &\rightarrow (12 \times 5) - (C_y \times 10) = 0 \rightarrow \boxed{C_y = 6 \text{ kips}} \\ \text{total } \sum \circlearrowleft M_B = 0 &\rightarrow (12 \times 5) + (18 \times 18) - 22 A_y = 0 \\ &\rightarrow \boxed{A_y = 24 \text{ kips}} \end{aligned}$$

$$\text{Check: } \uparrow \sum F_y = 0 \rightarrow 24 - 18 - 6 + 6 - 12 + 6 = 0 \quad 0 = 0 \quad \text{O.K.}$$

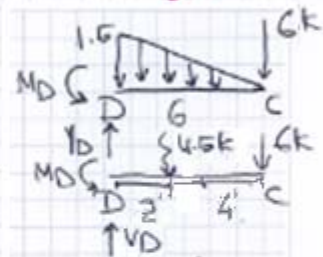
$$\sum \circlearrowleft M_A = (18 \times 4) + (6 \times 12) = 144 \text{ kips.ft}$$

(V)

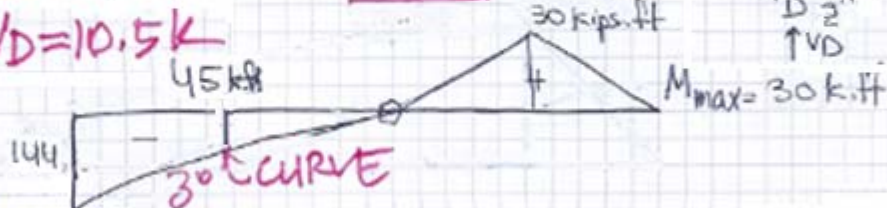


$$\text{Shear force at D} = V_D = 4.5 + 6 = 10.5 \text{ kips}$$

$$V_D = 10.5 \text{ k}$$



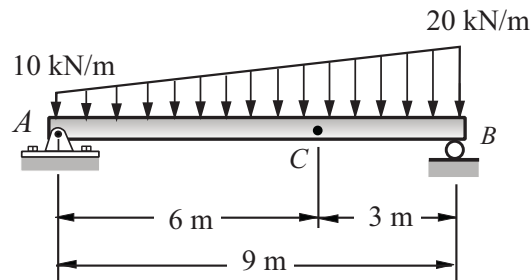
(M)



$$\text{Bending moment at D} \quad M_D = 0$$

$$(4.5) \times (2) + (6 \times 6) = 9 + 36 = 45 \text{ kips.ft}$$

Problem: (Determinate Beams)



FE/PE
EXAM

Support *A* : Pin
Support *B* : Roller

The dimensions and loading of a simple beam are given as shown. Using the listed data, answer the following questions:

(1) the support reaction (kN) at support *A* is most nearly

- (A) 60
- (B) 65
- (C) 70
- (D) 85

(2) the support reaction (kN) at right support *B* is most nearly

- (A) 85
- (B) 75
- (C) 65
- (D) 90

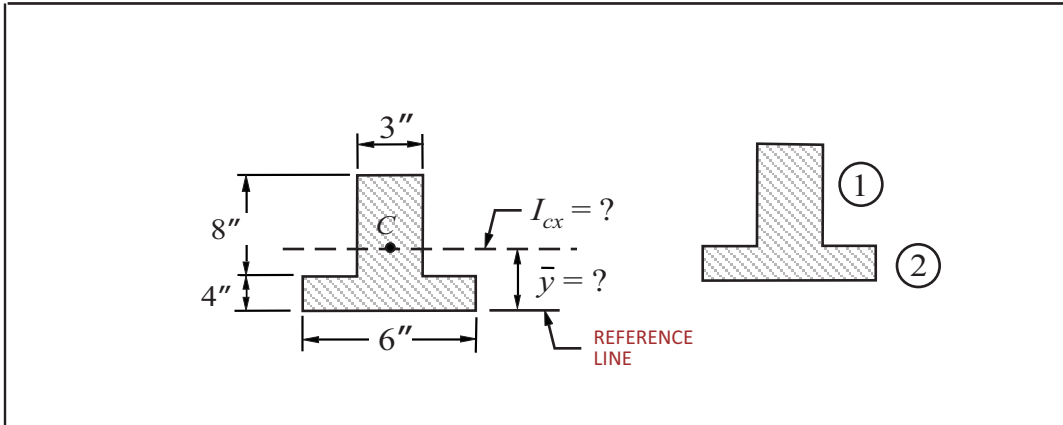
(3) the internal shear (kN) at point *C* is most nearly

- (A) +30.0
- (B) + 20.0
- (C) -30.0
- (D) -20.0

(4) the bending moment (kN.m) at point *C* is most nearly

- (A) 120
- (B) 130
- (C) 140
- (D) 150

Centroid / Moments of Inertia



Centroid Calculations

	A_i	y_i	$A_i y_i$
	in. ²	in.	in. ³
1	24.00	8.0	192.00
2	24.00	2.0	48.00
Σ	48.00	—	240.00

$$\bar{y} = \frac{\Sigma A_i y_i}{\Sigma A_i} = \frac{240}{48} = 5.0 \text{ in.}$$

Moments of Inertia

	I_o	A_i	d_i	$A_i d_i^2$
	in. ⁴	in. ²	in.	in. ⁴
1	128.0	24.00	3.00	216.00
2	32.00	24.00	3.00	216.00
Σ	160.00		—	432.00

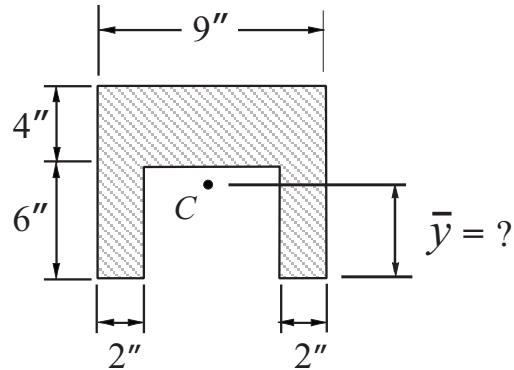
$$I_{xc} = \Sigma I_o + \Sigma A_i \cdot d_i^2 = 160.0 + 432.0 = 592 \text{ in.}^4$$

$$I_{yc} = I_{y1} + I_{y2} = 18.0 + 72.0 = 90.0 \text{ in.}^4$$

FUNDAMENTALS OF ENGINEERING

DOMAIN: STATICS

NCEES Reference Handbook / Page 63



FE/PE
EXAMS

The dimensions of a composite area are given as shown in the figure. Using the listed data answer the following questions:

(1) the distance \bar{y} (in.) of the centroid is most nearly

- (A) 7.30
- (B) 7.82
- (C) 6.75
- (D) 6.00



$$\bar{y} = ?$$

(2) the moment of inertia (in.^4) about the horizontal centroidal axis is most nearly (I_{cx})

- (A) 642
- (B) 504
- (C) 480
- (D) 395



$$I_{cx} = ?$$

(3) the moment of inertia (in.^4) about the vertical centroidal axis is most nearly (I_{cy})

- (A) 468
- (B) 545
- (C) 648
- (D) 735

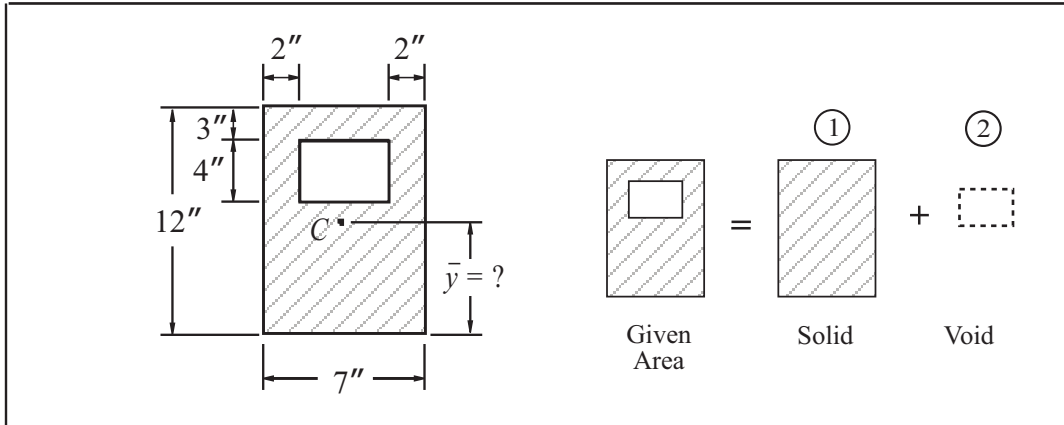


$$I_{cy} = ?$$

Answers

- 1- (D)
- 2- (C)
- 3- (B)

Centroid / Moments of Inertia



Centroid Calculations

	A_i in. ²	y_i in.	$A_i y_i$ in. ³
1	84.00	6.0	504.00
2	-12.00	7.0	-84.00
Σ	72.00	—	420.00

$$\bar{y} = \frac{\Sigma A_i y_i}{\Sigma A_i} = \frac{420}{72} = 5.83 \text{ in.}$$

Moments of Inertia Calculations

	I_o in. ⁴	A_i in. ²	d_i in.	$A_i d_i^2$ in. ⁴
1	1008	84.00	0.17	2.43
2	-16.00	-12.00	1.17	-16.43
Σ	992.0		—	-14.00

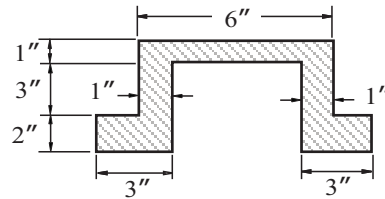
$$I_{cx} = \Sigma I_o + \Sigma A_i \cdot d_i^2 = 992 - 14 = 978 \text{ in.}^4$$

$$I_{cy} = I_{y1} + I_{y2} = \frac{12 \times 7^3}{12} - \frac{4 \times 3^3}{12} = 343 - 9 = 334 \text{ in.}^4$$

CENTROIDS / MOMENTS OF INERTIA

PARTIAL ANSWERS FOR SUPPLEMENTAL PROBLEMS

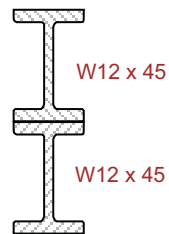
1- DEF-59



$$\bar{y} = 2.75 \text{ in.}$$

$$I_{cx} = 94.5 \text{ in.}^4$$

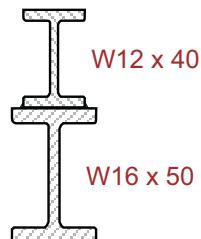
2- DEF-77



$$\bar{y} = 12.1 \text{ in.}$$

$$I_{cx} = 1655 \text{ in.}^4$$

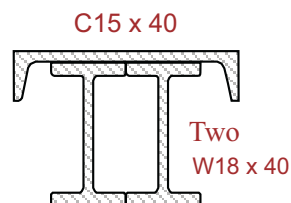
3- DEF-87



$$\bar{y} = 14.40 \text{ in.}$$

$$I_{cx} = 2261 \text{ in.}^4$$

4- DEF-91



$$\bar{y} = 11.85 \text{ in.}$$

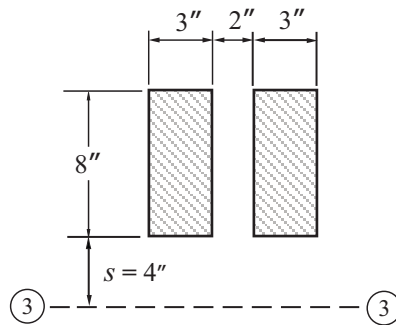
$$I_{cx} = 1827 \text{ in.}^4$$

CENTROIDS / MOMENTS OF INERTIA

SUPPLEMENTAL PROBLEMS

MORE PRACTICE APPLICATIONS

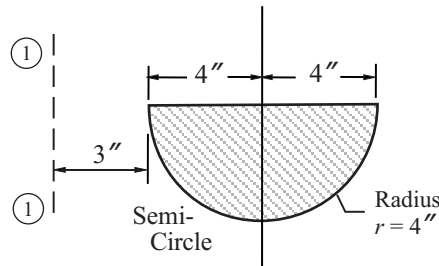
1-



$$I_{cx} = \dots\dots \text{in.}^4$$

$$I_{3-3} = 3328 \text{ in.}^4$$

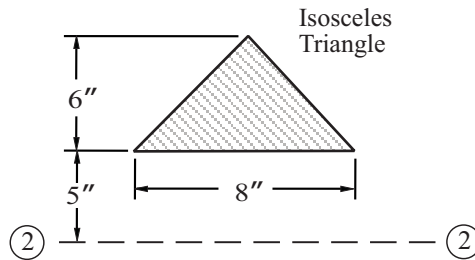
2-



$$I_{cx} = \dots\dots \text{in.}^4$$

$$I_{1-1} = 1332 \text{ in.}^4$$

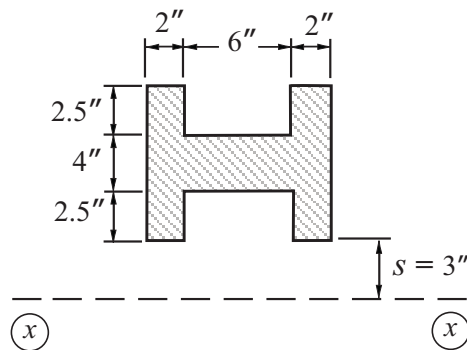
3-



$$I_{cx} = \dots\dots \text{in.}^4$$

$$I_{2-2} = 1224 \text{ in.}^4$$

4-



$$I_{cx} = 275 \text{ in.}^4$$

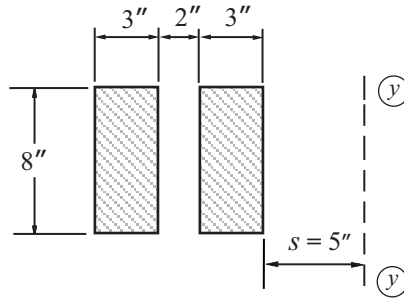
$$I_{x-x} = 3650 \text{ in.}^4$$

CENTROIDS / MOMENTS OF INERTIA

SUPPLEMENTAL PROBLEMS

MORE PAT APPLICATIONS

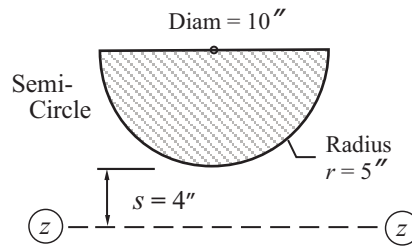
5-



$$I_{cx} = 336 \text{ in.}^4$$

$$I_{y-y} = 4224 \text{ in.}^4$$

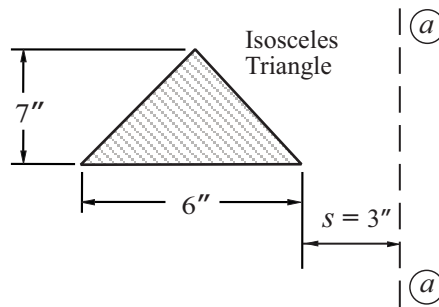
6-



$$I_{cx} = \dots \text{ in.}^4$$

$$I_{z-z} = 1927 \text{ in.}^4$$

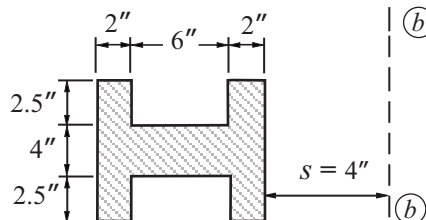
7-



$$I_{cy} = 31.5 \text{ in.}^4$$

$$I_{a-a} = 787.5 \text{ in.}^4$$

8-



$$I_{cy} = \dots \text{ in.}^4$$

$$I_{b-b} = 5520 \text{ in.}^4$$